

Circle Theorems Questions And Answers Complete Guide

circle theorems questions and answers are an essential part of geometry, especially in the study of circles. Understanding these theorems and mastering how to apply them through practice questions is crucial for students aiming for excellence in mathematics. Whether you're preparing for exams or seeking to strengthen your grasp on circle geometry, this comprehensive guide will walk you through common questions, detailed answers, and tips for solving circle theorems problems.

Introduction to Circle Theorems

Circle theorems are a set of rules that describe the relationships between angles, chords, tangents, and arcs within a circle. They are fundamental in solving geometric problems involving circles, and mastering them can significantly improve problem-solving efficiency and accuracy.

Common Types of Circle Theorems Questions

Circle theorems questions typically involve:

- Identifying angles formed by tangents, chords, and secants
- Applying the properties of angles subtended by the same arc
- Using the cyclic quadrilateral properties
- Calculating angles between tangents and chords
- Proving relationships involving diameters, radii, and chords

Below are some typical question types along with their solutions.

Sample Circle Theorems Questions and Answers

Question 1: Angle between a tangent and a chord

In a circle, a tangent AB touches the circle at point A. A chord AC intersects the circle at point C. If the angle between the tangent AB and the chord AC is 40° , what is the measure of angle ACB?

Answer 1:

The key to solving this problem lies in the tangent-chord angle theorem, which states:

- The angle between a tangent and a chord at the point of contact is equal to the angle subtended by the chord in the alternate segment of the circle.

Solution steps:

- Recognize that the angle between the tangent AB and the chord AC is 40° , so:

$$\angle BAC = 40^\circ$$

- According to the tangent-chord theorem:

$$\angle BAC = \angle ACB$$

- Therefore, the measure of $\angle ACB$ is 40° .

Final answer: $\boxed{40^\circ}$

Question 2: Opposite angles in a cyclic quadrilateral

In a cyclic quadrilateral ABCD, if $\angle ABC = 110^\circ$, what is the measure of $\angle ADC$?

Answer 2:

Properties of cyclic quadrilaterals tell us that:

- The sum of each pair of opposite angles is 180° .

Solution steps:

- Since ABCD is cyclic:

$$\angle ABC + \angle ADC = 180^\circ$$

- Given $\angle ABC = 110^\circ$:

$$\angle ADC = 180^\circ - 110^\circ = 70^\circ$$

Final answer: $\boxed{70^\circ}$

Question 3: Angles subtended by the same arc

In a circle, points P and Q lie on the circle such that both subtend an angle of 50° at a point on the circle. What is the measure of the angle between the lines PQ and the diameter passing through P and Q?

Answer 3:

This question involves understanding the properties of angles subtended by the same arc and how diameters relate to angles in a circle.

Solution steps:

- Since both points P and Q subtend a 50° angle at some point on the circle, by the equal angles theorem, the arcs subtended by these angles are equal.
- The key is to recognize that when a diameter is involved, the angle subtended by a diameter at the circumference is a right angle (90°).
- The angle between the chord PQ and the diameter passing through P and Q is related to the inscribed angles and their intercepts.
- The angle between the line PQ and the diameter passing through P and Q is 90° , because:
 - The diameter subtends a right angle at any point on the circle (Thales' theorem).

Final answer: $\boxed{90^\circ}$

Additional Important Circle Theorems and Their Applications

Understanding the core theorems helps in solving complex questions efficiently. Here are some fundamental circle theorems:

- **Angle at the Center vs. Angle at the Circumference:** The angle subtended at the center of a circle by a chord is twice the angle subtended at any point on the circumference.
- **Angles in a Semi-circle:** Any angle inscribed in a semi-circle is a right angle (90°).
- **Opposite Angles in Cyclic Quadrilaterals:** Opposite angles sum to 180° .
- **Tangents and Chords:** The angle between a tangent and a chord equals the inscribed angle subtended by the chord in the opposite segment.
- **Equal Arcs and Equal Angles:** Equal arcs subtend equal angles at the circumference.

Tips for Solving Circle Theorems Questions

- Always identify the given elements: radii, diameters, chords, tangents, and angles.
- Use the properties of angles subtended by the same arc: they are equal.
- Remember key theorems: Thales' theorem, the alternate segment theorem, cyclic quadrilateral properties.
- Draw diagrams carefully: accurate diagrams help visualize relationships.
- Label all known angles and arcs: helps in applying theorems systematically.
- Check for special cases: diameter, tangent points, or symmetric configurations.

Practice Problems for Mastery

To strengthen your understanding, try solving these additional circle theorems questions:

- In a circle, AB is a diameter, and C is a point on the circle. If $\angle ACB = 60^\circ$, find the measure of $\angle ABC$.
- Prove that the opposite angles of a cyclic quadrilateral are supplementary.
- In a circle, two chords AB and CD intersect at point E inside the circle. If $\angle AEB = 70^\circ$, find $\angle CED$.

Conclusion

Mastering circle theorems questions and answers is vital for excelling in geometry. By understanding core theorems, practicing a variety of problems, and applying logical reasoning, students can confidently tackle circle-related questions in exams. Remember to approach each problem systematically, use diagrams, and recall the key properties discussed. With consistent practice, you'll develop both speed and accuracy, making circle geometry an area where you feel confident and well-prepared.

Keywords for SEO optimization: circle theorems questions and answers, circle geometry problems, circle theorems examples, circle theorems solution, cyclic quadrilaterals, tangent-chord theorem,

angles in a circle, geometry practice questions

Circle Theorems Questions and Answers are fundamental components of geometry that often appear in school examinations, competitive exams, and mathematical problem-solving practice. Mastery of circle theorems not only helps students excel academically but also deepens their understanding of geometric relationships and properties. This article provides an in-depth exploration of common circle theorems questions, detailed answers, explanations, and tips to approach these problems effectively.

Understanding the Significance of Circle Theorems

Circle theorems form the backbone of many geometric proofs and problem-solving strategies. They describe relationships between angles, chords, tangents, and secants within a circle. Recognizing and applying these theorems allows students to solve complex problems involving circles with confidence. The key features include:

- Foundation for advanced geometry: Many proofs and problems build upon basic circle theorems.
- Enhances problem-solving skills: Applying theorems correctly can simplify otherwise complex problems.
- Common in exams: A significant portion of geometry questions in exams involve circle theorems.

Common Circle Theorems and Related Questions

Below, we explore some of the most important circle theorems, along with typical questions asked, detailed solutions, and explanations.

1. The Angle at the Centre Theorem

Statement: The angle subtended by a chord at the center of a circle is twice the angle subtended by the same chord at any point on the remaining part of the circle.

Sample Question:

In a circle with center O, chord AB subtends a triangle with an inscribed point P on the circumference. If $\angle APB = 50^\circ$, find $\angle AOB$.

Answer & Explanation:

According to the theorem, the angle at the center ($\angle AOB$) is twice the angle at the circumference ($\angle APB$).

Thus,

$$\angle AOB = 2 \times \angle APB = 2 \times 50^\circ = 100^\circ.$$

Key Points:

- The theorem simplifies the calculation of central angles when the inscribed angles are known.
- It is fundamental for understanding relationships between inscribed and central angles.

Pros:

- Straightforward application.
- Widely applicable in problems involving arcs and angles.

Cons:

- Only applicable when the angles are subtended by the same chord.

2. The Angle in a Semicircle Theorem

Statement: The angle subtended by a diameter at the circumference is a right angle (90°).

Sample Question:

Given a circle with diameter AB, point P lies on the circle. Find $\angle APB$.

Answer & Explanation:

Since AB is the diameter, any point P on the circle (other than A and B) will subtend a right angle at P.

Therefore, $\angle APB = 90^\circ$.

Features:

- Emphasizes the special case of semicircles.
- Useful in identifying right angles in circle problems.

Pros:

- Easy to remember and apply.
- Quick way to determine right angles.

Cons:

- Limited to cases involving diameters.

3. The Alternate Segment Theorem

Statement: The angle between a tangent and a chord at the point of contact is equal to the angle in the alternate segment.

Sample Question:

In a circle, a tangent at point T touches chord AC at T. If $\angle ATB$ is 60° , find the measure of the angle between the tangent and chord at T.

Answer & Explanation:

According to the theorem, the angle between the tangent and the chord ($\angle TTB$) equals the angle in the opposite segment, which is $\angle ACB$.

If $\angle ATB$ is 60° , then the angle between the tangent and the chord at T is also 60° .

Features:

- Connects tangent and chord angles effectively.
- Useful for solving problems involving tangents.

Pros:

- Simplifies the calculation of tangent-chord angles.

- Enhances understanding of the relationship between segments.

Cons:

- Requires correct identification of the segments involved.

4. The Cyclic Quadrilateral Theorem

Statement: Opposite angles of a cyclic quadrilateral sum to 180° .

Sample Question:

In a cyclic quadrilateral ABCD, $\angle A = 110^\circ$, find $\angle C$.

Answer & Explanation:

Since ABCD is cyclic, opposite angles sum to 180° .

$$\angle A + \angle C = 180^\circ,$$

$$110^\circ + \angle C = 180^\circ,$$

$$\angle C = 70^\circ.$$

Features:

- Critical for problems involving quadrilaterals inscribed in circles.
- Helps in establishing angle relationships.

Pros:

- Straightforward in calculation.
- Widely applicable in geometry problems.

Cons:

- Only applies to cyclic quadrilaterals.

Advanced Circle Theorem Questions

While the above theorems are foundational, advanced problems often combine multiple theorems and require deeper reasoning.

5. Combining Theorems for Complex Problems

Sample Question:

In a circle, chord AB subtends a 60° angle at the circumference. The same chord subtends an angle at the center. Find the measure of the angle between the tangent at point A and the chord AB.

Answer & Explanation:

First, determine the central angle subtended by chord AB.

From the Angle at the Center Theorem,

$$\angle AOB = 2 \times 60^\circ = 120^\circ.$$

Next, the tangent at A forms an angle with chord AB equal to the angle in the alternate segment, which is $\angle ACB$ (assuming C is a point on the circle forming the triangle). Alternatively, in many configurations, this tangent-chord angle is related directly to the inscribed angles.

Using the Alternate Segment Theorem, the angle between the tangent at A and chord AB is equal to $\angle ACB$, which can be calculated based on the properties of the circle.

Features:

- Demonstrates the power of combining multiple theorems.
- Encourages logical reasoning.

Pros:

- Builds problem-solving versatility.
- Prepares students for challenging exam questions.

Cons:

- Requires careful diagram analysis and multiple theorem applications.

Tips and Strategies for Solving Circle Theorems Questions

- Draw accurate diagrams: Visual representation simplifies understanding relationships.
- Identify knowns and unknowns: Clarify what the question provides and what needs to be found.
- Recall relevant theorems: Match problem features with applicable theorems.
- Look for symmetry: Symmetry often simplifies angle relationships.
- Use supplementary and complementary angles: Remember that angles in a straight line sum to 180° , and angles in a triangle sum to 180° .
- Practice with varied problems: Exposure to different question types improves problem-solving skills.

Pros and Cons of Focused Practice on Circle Theorems

Pros:

- Builds a strong conceptual understanding.
- Improves speed and accuracy in exams.
- Enhances geometric intuition.

Cons:

- Can be challenging without visual aids.
- Over-reliance on memorization rather than understanding may limit problem-solving flexibility.

Conclusion

Circle theorems questions and answers are integral to mastering geometry. They reinforce core concepts about angles, chords, tangents, and cyclic quadrilaterals, forming the foundation for more advanced geometric reasoning. By practicing a variety of questions and understanding their underlying principles, students can develop both confidence and competence in tackling circle-based problems. Whether for school exams or competitive tests, a thorough grasp of circle theorems significantly boosts mathematical problem-solving skills and overall geometric insight.

Question What is the Inscribed Angle Theorem in circle geometry? The Inscribed Angle Theorem states that an angle inscribed in a circle is half the measure of the intercepted arc it subtends. How can you prove that the opposite angles of a cyclic quadrilateral sum to 180 degrees?

In a cyclic quadrilateral, the opposite angles are supplementary because each pair of opposite angles intercepts the same arc or supplementary arcs, summing to 180 degrees. What is the relationship between the angles in a tangent and a chord in a circle? The angle between a tangent and a chord is equal to the inscribed angle subtended by the same chord on the alternate segment of the circle. How do you determine the angle between two intersecting chords inside a circle? The angle between two intersecting chords is half the sum of the measures of the arcs intercepted by the angles and their vertically opposite angles. What is the significance of the alternate segment theorem? The alternate segment theorem states that the angle between a tangent and a chord is equal to the angle in the alternate segment, which helps in solving various circle geometry problems. How can you prove that the diameter of a circle subtends a right angle to any point on the circle? Using Thales' theorem, which states that any angle subtended by a diameter at the circumference of a circle is a right angle (90 degrees). What is the key property of angles in a cyclic quadrilateral? The key property is that the sum of the measures of opposite angles in a cyclic quadrilateral is 180 degrees. How do you find the measure of an angle in a circle when given the intercepted arcs? The measure of an inscribed angle is half the measure of the intercepted arc, while for a central angle, it equals the measure of the intercepted arc. What is the role of the tangent-chord angle in circle theorems? The tangent-chord angle theorem states that the angle between a tangent and a chord is equal to the inscribed angle in the alternate segment, which is useful to find unknown angles. Can you explain the concept of cyclic triangles and their relation to circle theorems? A cyclic triangle is a triangle inscribed in a circle, where the vertices lie on the circle, and properties like equal angles subtended by the same arc help solve related geometry problems.

Related keywords: circle theorems, geometry, angles in circles, cyclic quadrilaterals, inscribed angles, tangent and radius, chord properties, cyclic quadrilaterals questions, circle geometry problems, circle theorem formulas

Geometry Review Sheet Circle Vocabulary Central And

geometry review sheet circle vocabulary central and understanding the fundamental concepts and vocabulary related to circles is essential for mastering geometry. Circles are one of the most intriguing shapes in mathematics, characterized by their perfect symmetry and unique properties. Whether you're a student preparing for an exam, a teacher designing lesson plans, or a math enthusiast looking to deepen your knowledge, a solid grasp of circle-related vocabulary is crucial. This review sheet aims to clarify key terms and concepts associated with circles, focusing on the central ideas and their applications in geometry.

Fundamental Circle Vocabulary

Understanding the basic vocabulary related to circles forms the foundation for more advanced topics. Here are some of the most important terms to know:

Circle

A circle is a set of all points in a plane that are equidistant from a fixed point called the center. The distance from the center to any point on the circle is called the radius.

Center

The fixed point inside the circle from which all points on the circle are equally distant. The center is often labeled as O.

Radius

A line segment connecting the center of the circle to any point on the circle. All radii in a circle are equal in length.

Diameter

A line segment passing through the center and connecting two points on the circle. It is twice as long as the radius: $D = 2r$.

Chord

A line segment with both endpoints on the circle. A diameter is a special type of chord.

Arc

A portion of the circumference of a circle. Arcs are named by their endpoints, for example, AB.

Sector

A region bounded by two radii and an arc, resembling a "slice" of the circle.

Segment

A region bounded by a chord and the corresponding arc.

Circumference

The distance around the circle. It can be calculated using the formula: $C = 2\pi r$ or $C = \pi d$.

Key Properties and Relationships

Understanding the properties and relationships between the various parts of a circle allows for problem-solving and geometric proofs.

Central and Inscribed Angles

- Central Angle: An angle whose vertex is at the center of the circle and whose sides intersect the circle. The measure of a central angle is equal to the measure of its intercepted arc.
- Inscribed Angle: An angle whose vertex is on the circle and whose sides intersect the circle. The measure of an inscribed angle is half the measure of its intercepted arc.

Arc Measures

- The measure of an arc is proportional to the central angle that intercepts it.
- For a full circle, the sum of the measures of all arcs equals 360° .

Relationship Between Chords, Secants, and Tangents

- Chord: A segment with both endpoints on the circle.
- Secant: A line that intersects the circle at two points.
- Tangent: A line that touches the circle at exactly one point, called the point of tangency.

Special Lines in Circles

Certain lines have specific properties that are vital in circle geometry.

Tangent Line

A line that touches the circle at exactly one point. The tangent is perpendicular to the radius drawn to the point of tangency.

Secant Line

A line that intersects the circle at two points, creating intersecting chords or segments.

Chord and Diameter Relationships

- The diameter bisects chords that are perpendicular to it.
- The longest chord in a circle is the diameter.

Important Theorems and Formulas

Familiarity with key theorems helps in solving complex problems involving circles.

Thales' Theorem

If A, B, and C are points on a circle where AC is a diameter, then the angle ABC is a right angle.

Chord Distance Formula

The perpendicular distance from the center to a chord can be found using:

$$d = \sqrt{r^2 - \left(\frac{c}{2}\right)^2}$$

where d is the distance from the center, r is the radius, and c is the length of the chord.

Area of a Sector

The area of a sector with central angle θ (in degrees) is:

$$\text{Area} = \frac{\theta}{360^\circ} \times \pi r^2$$

Arc Length Formula

The length of an arc with central angle θ is:

$$\text{Arc Length} = \frac{\theta}{360^\circ} \times 2\pi r$$

Applications and Problem-Solving Strategies

Applying these vocabulary terms and properties allows for effective problem-solving in various contexts.

Identifying Key Components

When presented with a circle problem, first identify:

- The center
- The radii
- Any chords, secants, or tangents
- The angles involved

Using Theorems to Find Unknowns

Apply theorems such as:

- Central and inscribed angle relationships
- Thales' theorem
- Properties of tangents and radii

Calculating Lengths and Areas

Use the relevant formulas for circumference, area of sectors, and arc lengths based on given measurements.

Practice Problems for Reinforcement

To solidify understanding, here are some practice problems:

- Find the length of an arc if the central angle measures 60° in a circle with radius 10 units.
- Given a circle with diameter 14 cm, find the circumference and the area.
- In a circle, if an inscribed angle intercepts an arc of 80° , what is the measure of the inscribed angle?
- Determine the length of a chord if the distance from the center to the chord is 5 units, and the radius of the circle is 13 units.
- Prove that the tangent to a circle is perpendicular to the radius at the point of tangency.

Conclusion

Mastering the vocabulary associated with circles is a vital step in understanding and solving geometry problems. From basic components like the radius and diameter to more complex concepts like central and inscribed angles, a comprehensive grasp of these terms provides clarity and confidence. Regular practice, coupled with an understanding of the key theorems and formulas, will

enhance your ability to analyze and solve a wide array of circle-related problems. Remember, the beauty of circle geometry lies in its symmetry and the elegant relationships between its parts?knowing the vocabulary unlocks the door to appreciating its full mathematical elegance.

Geometry Review Sheet Circle Vocabulary Central and

Understanding the fundamental vocabulary related to circles is essential for mastering geometry concepts. The terms surrounding circles?such as radii, diameters, chords, tangents, sectors, and arcs?form the building blocks of more complex geometric reasoning. In this review, we will explore the key vocabulary associated with circles, with a focus on the central concepts that underpin circle geometry, providing clarity and insight into their definitions, properties, and interrelationships.

Introduction to Circle Geometry Vocabulary

Circles are one of the most fundamental shapes in geometry, characterized by a set of points equidistant from a fixed point called the center. To describe and analyze circles effectively, mathematicians have developed a precise vocabulary. These terms help describe the relationships between different parts of a circle and are vital for solving problems related to area, circumference, angles, and more.

Key Terms and Definitions

Understanding the vocabulary associated with circles begins with familiarizing oneself with the core components. Here are the most essential terms:

Center

- The fixed point inside a circle from which every point on the circle is equidistant.
- Denoted as point O or C in diagrams.

Radius

- A segment drawn from the center of the circle to any point on the circle.
- All radii in a circle are equal in length.
- Commonly denoted as r .

Diameter

- A chord that passes through the center of the circle.
- The longest chord in the circle.
- Equals twice the radius ($d = 2r$).
- Denoted as d .

Chord

- A segment with both endpoints on the circle.
- Does not necessarily pass through the center.
- Examples include minor and major chords, depending on their length relative to the circle.

Secant

- A line that intersects the circle at two points.
- Extends infinitely in both directions.

Tangent

- A line that touches the circle at exactly one point.
- The point of contact is called the point of tangency.

Arc

- A portion of the circle's circumference.
- Defined by two endpoints on the circle.
- Can be classified as a minor arc (less than 180°) or a major arc (more than 180°).

Central Angle

- An angle whose vertex is at the center of the circle, with sides intersecting the circle.
- Measures the degree of the arc it intercepts.

Inscribed Angle

- An angle with its vertex on the circle and sides intersecting the circle.

- The intercepted arc is opposite the angle.

Sector

- A "slice" of the circle, formed by two radii and the connecting arc.
- Similar to a wedge-shaped region.

Segment

- A region bounded by a chord and the arc it subtends.
- Can be thought of as a "slice" of the circle, excluding the central angle.

Deep Dive into Circle Vocabulary: Properties and Relationships

Understanding how these components relate is crucial for geometric proofs and problem-solving.

The Relationship between Radius, Diameter, and Circumference

- The radius (r) is fundamental; all radii are equal.
- The diameter (d) is twice the radius: $d = 2r$.
- The circumference (C) of a circle is calculated as $C = 2\pi r$, or $C = \pi d$.

Chords and Their Properties

- Perpendicular bisectors: The perpendicular bisector of a chord passes through the circle's center.
- Equal chords: Chords equidistant from the center are equal in length.
- Longest chord: The diameter is the longest chord.

Angles in Circles

- Central angles: Measure the intercepted arc directly; an angle at the center.
- Inscribed angles: Measure half the intercepted arc; important in proving circle theorems.
- Angles formed by tangents and chords: The measure of such an angle equals half the measure of the intercepted arc.

Arcs and Their Measures

- The measure of a minor arc equals the measure of its central angle.
- The measure of a major arc is greater than 180° .
- The measure of a semicircular arc (half the circle) is 180° .

Sectors and Segments

- The area of a sector is proportional to its central angle: $\text{Area} = \frac{\theta}{360^\circ} \times \pi r^2$.
- A segment's area can be found by subtracting the area of the triangle formed by the radii from the sector's area.

Special Lines and Their Significance

Certain lines and points are crucial for understanding circle properties.

Tangent Lines

- Touch the circle at only one point.
- Are perpendicular to the radius at the point of tangency.
- Play a key role in circle theorems, such as the tangent-chord theorem.

Secants and External Points

- When a secant line passes outside the circle, it forms two segments with the circle.
- The power of a point theorem relates secants and tangents intersecting outside the circle.

Points of Tangency and Contact

- The unique point where a tangent touches the circle.
- The basis for many angle and length theorems involving tangents.

Common Theorems and Their Vocabulary Connections

The vocabulary is often used to state and prove fundamental circle theorems:

- Theorem 1: The measure of an inscribed angle is half the measure of its intercepted arc.
- Theorem 2: Tangent line perpendicular to the radius at point of tangency.
- Theorem 3: Chords equidistant from the center are equal in length.
- Theorem 4: The angles between a tangent and a chord are equal to the inscribed angles subtended by the same arc.

Practical Applications and Problem-Solving Strategies

When approaching circle problems, correctly identifying and utilizing the vocabulary terms can streamline reasoning:

- Recognize whether a line is a tangent, secant, or chord.
- Identify central and inscribed angles and their intercepted arcs.
- Use properties of equal chords and radii to find unknown lengths.
- Apply sector and segment formulas when calculating areas.
- Leverage the relationships between angles and arcs to set up equations.

Mastering the vocabulary of circle geometry is indispensable for students and enthusiasts aiming to deepen their understanding of this fundamental shape. By internalizing terms like radius, diameter, chord, tangent, arc, sector, and their related properties, learners can unlock a wealth of geometric truths and solve complex problems with confidence. As with any mathematical domain, language shapes understanding, so developing a robust "circle vocabulary" lays a solid foundation for future explorations in geometry and beyond.

Remember: Visual diagrams are invaluable. Always accompany these terms with sketches to enhance comprehension and retention. Whether you're reviewing for a test or exploring advanced topics, a strong grasp of circle vocabulary is your gateway to geometric mastery.

Question What is the definition of a circle's radius? The radius of a circle is the distance from the center of the circle to any point on its circumference. What does the term 'central angle' mean in circle geometry? A central angle is an angle whose vertex is at the center of the circle and whose sides intersect the circle at two points. How is a diameter related to the circle's radius? A diameter is twice the length of the radius; it passes through the circle's center and touches two points on the circumference. What is the meaning of 'circle vocabulary' in geometry? Circle vocabulary includes terms like radius, diameter, circumference, arc, chord, central angle, and sector, which describe different parts and properties of a circle. Why is understanding central angles important in circle geometry? Understanding central angles helps in calculating the measures of arcs, sectors, and in solving problems related to circle segments and their properties.

Related keywords: circle, radius, diameter, circumference, chord, arc, tangent, secant, central

angle, vocabulary

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